KS2 Expectations
Multiples and factors

- Relating multiplication \& division as inverses

Scaling problems with measures

- With integer and unit fraction scale factors only - e.g., twice as long, half as tall Scaling drawings and similarity
- Lengths, with integer and unit fraction scale factors only

Ratio

- Unequal sharing
- In the form of 'for every ..., there are ..."

Fractions

- Equivalent Fractions
- Multiplication of an integer by unit fraction (integer product)
- Multiplication of proper fractions
- Division of a proper fraction by an integer

| Ratio Tables |  |
| :---: | :---: |
| Year 11 | Using Graphs Multiplicate Reasoning |
| Year 10 | Congruence, similarity \& enlargement <br> Trigonometry <br> Ratios \& Fractions |
| Year 9 | Straight line graphs Using Percentages Maths and Money Enlargement \& Similarity Ratio \& Proportion Rates |
| Year 8 | Ratio \& Scale <br> Multiplicative Change <br> Fractions \& Percentages <br> Number Sense |
| Year 7 | FDP Equivalence <br> Multiplication \& Division <br> Fractions \& Percentages of Amounts <br> Construction \& Measuring |

We need the structure of the ratio table to be familiar to students, before using it with novel concepts or concepts they may not have fully grasped yet.
Resources for this are here: Don Steward Task MathsBot


## Year 8

Ratio \& Scale

- Express ratios in their simplest integer form

$$
30: 10
$$

$$
3: 1
$$



- Solve problems involving the ratio m:n

The ratio of adults to children at a cricket match is 7:3 There 150 people at the match. How many children attended the cricket match?



James has some apples and oranges.
The ratio of apples and oranges is 2:5
He has 15 oranges. 6
How many apples does James have?

The ratio of Mollie's age to Heather's age is 4:9 Heather is 40 years older than Mollie How old is Mollie? 32


- Express ratios in the form $1: \mathrm{n}$ and $\mathrm{n}: 1$
$15: 10$

- Understand gradient of a line as a ratio (H)

- Understand $\pi$ as the ratio between diameter and circumference



## Multiplicative Change

- Solve problems involving direct proportion

5 scoops of ice cream costs $£ 4.50$. How much would it cost for:
$\square 10$ scoops
$\square 8$ scoops
$\square 9$ scoops

serves 4
300 ml double cream 320 ml milk 120 g caster sugar 1 vanilla pod

3 people?


- Explore conversion graphs

Use the fact 5 miles $=8$ kilometres to draw a conversion graph on the grid.



- Convert between currencies


George is going on holiday to Poland
George changes £120 into Zloty. The exchange rate is $£ 1=5$ Zloty

- Ratio between similar shapes

- Understand scale factors as multiplicative representations
6 cm



Draw \& interpret scale diagrams
Draw a plan of this room using a scale of $1: 50$.


- Interpret maps using scale factors and ratios

A map has a scale of 1:4000
On the map, the distance between two houses is 9 cm .
What is the actual distance between the houses? Give your answer in metres.


Fractions \& Percentages

- Calculate percentage increase \& decrease using a multiplier

Increase 80 ml by 9\%


Decrease 40 by 10\%

$\times 0.9$| 40 | $100 \%$ |
| :---: | :---: |
| 36 | $90 \%$ |

- Express one number as a fraction or percentage of another

Write $£ 6$ as a fraction of $£ 875 \%$


Write 5 cm as a percentage of 20 cm


Write 22 as a percentage of 40


- Work with percentage change


A car is travelling at 40 kilometres per hour.
The car increases its speed to 56 kilometres per hour.
Calculate the percentage increase in the speed of the car.

- (H) Find the original amount given the percentages $<100 \%$
$20 \%$ of all the children in a class are left handed.
4 children are left handed.
How many children are there in the class altogether?

- (H) Find the original amount given the percentages > 100\%

Heather invested money into a savers bank account.
Each year the money in the account earns $10 \%$ interest.
After one year, the total amount of money in the account was $£ 2200$
How much did Heather invest?


## Number Sense

- Convert metric units of area \& volume

Convert $6.3 \mathrm{~m}^{2}$ to $\mathrm{cm}^{2}$


Convert $0.4 \mathrm{~m}^{3}$ into $\mathrm{cm}^{3}$

## Year 9

## Straight line graphs

- Compare gradient

See Year 8 in Ratio \& Scale - Understand gradient of a line as a ratio (H)
Using Percentages

- Solve reverse percentage problems

See Year 8 in Fractions \& Percentages - (H) Find the original amount given the percentages < 100\% and > 100\%

## Maths and Money

- Solve problems with Value Added Tax

Sinead buys a watch.
$20 \%$ VAT is added to the price of the watch.
Sinead then has to pay a total of $£ 60$
What is the price of the watch with no VAT added?


- Solve problems with exchange rates


Annie is going on holiday to Spain.
The exchange rate is $£ 1=€ 1.15$
She changes $£ 200$ into euros ( $€$ )
How many euros does she receive?

Annie comes back from holiday with €60 and changes these back into pounds.
The exchange rate is now $£ 1=€ 1.20$
Work out how many pounds Annie receives.


- Solve unit pricing problems


## Kate buys 6 pencils for 90 p.

How much do 11 pencils cost?
How much do 4 pencils cost?


## Enlargement \& Similarity

- Recognise enlargement \& similarity



Which triangles are similar?

- Work out missing sides in a pair of similar shapes

- (H) Solve problems with similar triangles

- Explore ratios in right-angled triangles (H)


Solving ratio \& proportion problems

- Solve problems with inverse proportion

- Solve 'best buy' problems

See Year 9 in Maths \& Money - solve unit pricing problems


How much is one lemon from the supermarket?
How much is one lemon from the greengrocer? Which offers better value for money?


Rates

- Speed, distance \& time

A lorry travels 120 miles in 3 hours 40 mph



A car travels at a speed of 44 mph for 15 minutes.

$\therefore$| 44 miles | 1 how |
| :--- | :--- |
| IImies | 15 mins |



A lorry drives 250 miles at a speed of 50 mph .

A car travels 100 miles at a speed of 40 mph .

- Density, mass \& volume


A piece of wood has a mass of 7 g and a volume of $10 \mathrm{~cm}^{3}$

$$
0.7 \mathrm{~g} / \mathrm{cm}^{3}
$$



A statue with a volume of $120 \mathrm{~cm}^{3}$ made from ceramic which has a density of $2 \mathrm{~g} / \mathrm{cm}^{3}$.


A 50 g piece of wood which has a density of $0.4 \mathrm{~g} / \mathrm{cm}^{3}$ $125 \mathrm{~cm}^{3}$

- Rates of change and their units

Scott types at an average rate of 40 words per minute.


How many words can Scott type in three-quarters of an hour? How long will it take Scott to type a 10000 word essay? 250 mins

- (H) Convert compound units

Change the following speeds into metres per second.

360km/h
$100 \mathrm{~m} / \mathrm{s}$


| 10 km | howr |
| :---: | :---: |
| (10000m | 60 min ) 60 |
| (166.6m | 1 min $\times=0$ |
| 166.6 m | 60 sees). |
| , 2.7 m | Isee |

$10 \mathrm{~km} / \mathrm{h}$
$2.7 \mathrm{~m} / \mathrm{s}$

Convert $5 \mathrm{~km} / \mathrm{h}$ into $\mathrm{m} / \mathrm{s}$.
$=60\left(\begin{array}{|c|c|}\hline 5 \mathrm{~km} & 1 \text { how } \\ \hline 5000 \mathrm{~m} & 60 \mathrm{mus} \\ \hline 83.3 \mathrm{~m} & 1 \mathrm{mu} \\ \hline 83.3 \mathrm{~m} & 60 \mathrm{sec}\end{array}\right)=60$

## Year 10

Congruence, similarity \& enlargement

- (H) Explore areas of similar shapes
$\left(2^{2}\right) \times 2\left(\begin{array}{|l|l|}\hline 3 \times 5 & 15 \\ \hline 6 \times 10 & 60 \\ \hline\end{array}\right) \times 2\left(2^{2}\right)$
$3 \mathrm{~cm} \square$
$6 \mathrm{~cm} \quad 10 \mathrm{~cm}$


$5^{000}$

- (H) Explore volumes of similar shapes


Volume $=160000 \mathrm{~cm}^{3}$



## Trigonometry

- Explore ratios in similar right-angled triangles



## Collecting, representing \& interpreting data

- Construct a stratified sample (H)

The table shows information about the inhabitants of a village.


Henry takes a stratified sample of 40 .
Work out the number of each age group that Henry should choose.

- Capture-Recapture method

Hannah wants to estimate the number of eels in a lake.
She catches and rings 50 eels.
She returns the 50 eels to the lake.
The next day Hannah catches 400 eels. Of these 400 eels, 10 are ringed.


Work out an estimate for the total number of eels in the lake.

Ronan wants to estimate the number of honey bees in a beehive.
On Wednesday, Ronan catches 660 honey bees from the beehive.
He marks the honey bees and then releases them.
On Thursday, Ronan catches 400 honey bees and notes how many were marked.
Ronan then calculates his estimate as 22,000 honey bees in the beehive.
How many of the 400 honey bees caught on Thursday were marked?


## Year 11

## Using Graphs

- Contrast \& interpret distance/time graphs

- Construct \& interpret speed/time graphs

- Recognise and interpret graphs that illustrate direct \& inverse proportion


$\times$ One ct Pap orion


Multiplicate reasoning

- Understand direct proportion

A is directly proportional to B .
When $\mathrm{A}=12$, $\mathrm{B}=3$
(a) Find a formula for $A$ in terms of $B$.
(b) Find the value of A when $\mathrm{B}=5$
(c) Find the value of B when $\mathrm{A}=36$


W is directly proportional to $\mathrm{P}^{3}$.
When $\mathrm{P}=2$, $\mathrm{W}=32$
(a) Express $W$ in terms of $P \quad W=P^{3}$
(b) What is the value of $W$ when $P=4$ ? 256
(c) What is the value of P when $\mathrm{W}=4000$ ?

$$
\sqrt[3]{1000}=10
$$

- Understand inverse proportion

T is inversely proportional to N .
When $\mathrm{T}=30, \mathrm{~N}=5$.
(a) Find an equation connecting $T$ and $N . \quad T N=150$
(b) Work out the value of $T$ when $N=10$ is
(c) Work out the value of N when $\mathrm{T}=256$


The force, $F$ newtons, exerted by a magnet on a metal object is inversely proportional to the square of the distance $d \mathrm{~cm}$

When the $d=2 \mathrm{~cm}, F=60 \mathrm{~N}$
(a) Express $F$ in terms of $d$
$F=240$
(b) Find the force when the distance between the magnet and the metal object is $10 \mathrm{~cm} \quad 2.4 \mathrm{~N}$
(c) Find the distance between the magnet and the metal object when the force is 15 N .4 cm


## Ratio Tables

- Density

A piece of wood has a mass of 7 g and a volume of $10 \mathrm{~cm}^{3}$



A statue with a volume of $120 \mathrm{~cm}^{3}$ made from ceramic which has a density of $2 \mathrm{~g} / \mathrm{cm}^{3}$.



A 50 g piece of wood which has a density of $0.4 \mathrm{~g} / \mathrm{cm}^{3}$

- Pressure

A box is placed on a table and exerts a force of 250 N on an area of $20 \mathrm{~cm}^{2}$
$12.5 \mathrm{~N} / \mathrm{m}^{2}$


The area of contact is $16 \mathrm{~cm}^{2}$ and the pressure exerted is $10 \mathrm{~N} / \mathrm{cm}^{2}$


160 N

The object exerts a force of 420 N on the floor and the pressure on the floor is $20 \mathrm{~N} / \mathrm{cm}^{2}$



